

**JEE (MAIN)**

**TEST SERIES**

**SUBJECT : PHYSICS, CHEMISTRY, MATHEMATICS**

**TEST CODE : TSJMT220**

**QUESTION PAPER**

**TIME : 3 HRS**

**MARKS : 300**

**INSTRUCTIONS**

**GENERAL INSTRUCTIONS :**

1. This test consists of 75 questions.
2. There are three parts in the question paper A, B, C consisting of Physics, Chemistry and Mathematics having 25 questions in each part
3. 20 questions will be Multiple choice questions & 5 questions will have answer to be filled as numerical value.
4. Marking scheme :

Type of Questions	Total Number of Questions	Correct Answer	Incorrect Answer	Unanswered
MCQ's	20	+4	Minus One Mark(-1)	No Mark (0)
Numerical Values	5	+4	No Mark (0)	No Mark (0)

5. There is only one correct response for each question. Filling up more than one response in each question will be treated as wrong response and marks for wrong response will be deducted accordingly as per instruction 4 above.

**OPTICAL MARK RECOGNITION (OMR) :**

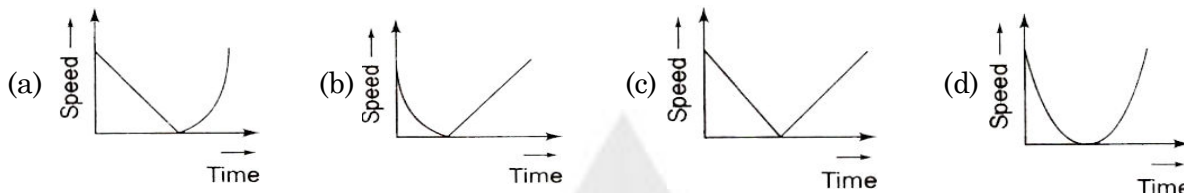
6. The OMR will be provided to the students.
7. Darken the appropriate bubbles on the OMR sheet by applying sufficient pressure.
8. The OMR sheet will be collected by the invigilator at the end of the examination.
9. Do not tamper with or mutilate the OMR. Do not use the OMR for rough work.
10. Write your name, Batch name, name of the center, Test Code, roll number and signature with pen in the space provided for this purpose on the OMR. Do not write any of these details anywhere else on the OMR.

**DARKENING THE BUBBLES ON THE OMR :**

11. Use a BLACK BALL POINT PEN to darken the bubbles on the OMR.
12. Darken the bubble COMPLETELY.
13. Darken the bubbles ONLY IF you are sure of the answer. There is NO WAY to erase or "un-darken" a darkened bubble.

## Part A - PHYSICS

- Q.1 The equation of state of some gases can be expressed as  $\left(P + \frac{a}{V^2}\right) = \frac{R\theta}{V}$ , where  $P$  is pressure,  $V$  volume,  $\theta$  absolute temperature and  $a$  and  $b$  are constants. The dimensional formula of  $a$  is  
 (a)  $[ML^5T^{-2}]$  (b)  $[M^{-1}L^5T^2]$  (c)  $[ML^{-1}T^2]$  (d)  $[ML^{-5}T^2]$
- Q.2 A ball is thrown vertically upwards. Which of the following plots represents the speed-time graph of the ball during its flight if the air resistance is not ignored?



- Q.3 The speed of a projectile at the highest point becomes  $1/\sqrt{2}$  time its initial speed. The horizontal range of the projectile will be

(a)  $\frac{u^2}{g}$  (b)  $\frac{u^2}{2g}$  (c)  $\frac{u^2}{3g}$  (d)  $\frac{u^2}{4g}$

- Q.4 A car A moves due north at a speed of 40 km/h. While another car B moves due east at a speed of 30 km/h. Find the velocity of car B relative to car A (both in magnitude and direction)

- (a) 40 km/h; at an angle  $\tan^{-1}\left(\frac{3}{5}\right)$  east of south  
 (b) 50 km/h; at an angle  $\tan^{-1}\left(\frac{3}{5}\right)$  east of south  
 (c) 40 km/h; at an angle  $\tan^{-1}\left(\frac{3}{4}\right)$  east of south  
 (d) 50 km/h; at an angle  $\tan^{-1}\left(\frac{3}{4}\right)$  east of south.

- Q.5 When forces  $F_1$ ,  $F_2$ , and  $F_3$  are acting on a particle of mass  $m$  such that  $F_2$  and  $F_3$  are mutually perpendicular, then the particle remains stationary. If the force  $F_1$  is now removed, then the acceleration of the particle is

(a)  $F_1/m$  (b)  $F_2F_3/mF_1$  (c)  $(F_2 - F_3)/m$  (d)  $F_2/m$

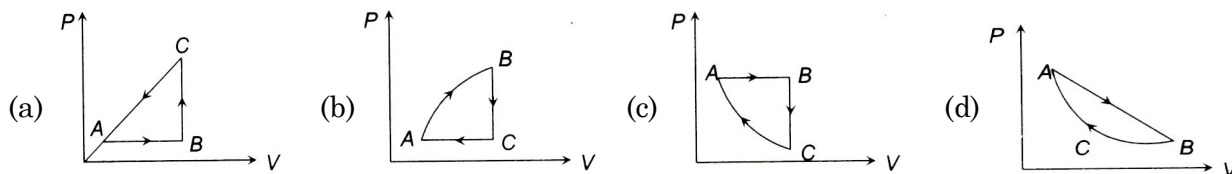
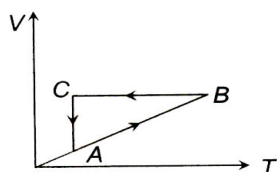
- Q.6 A heavy uniform chain lies on a horizontal table top. If the coefficient of friction between the chain and the table surface is 0.25, then the maximum fraction of the length of the chain that can hang over on edge of the table is

(a) 20% (b) 25% (c) 35% (d) 15%

- Q.7 The radii of two soap bubbles are  $R_1$  and  $R_2$ , respectively. The ratio of masses of air in them will be

(a)  $\frac{R_1^3}{R_2^3}$  (b)  $\frac{R_2^3}{R_1^3}$  (c)  $\left(\frac{P + \frac{4T}{R_1}}{P + \frac{4T}{R_2}}\right) \frac{R_1^3}{R_2^3}$  (d)  $\left(\frac{P + \frac{4T}{R_2}}{P + \frac{4T}{R_1}}\right) \frac{R_2^3}{R_1^3}$

Q.8 A cycle process ABCA is shown in figure Process on the  $P - V$  diagram is



Q.9 A thermally insulated vessel contains an ideal gas of molecular mass  $M$  and ratio of specific heats  $\gamma$ . It is moving with speed  $v$  and is suddenly brought to rest. Assuming no heat is lost to the surrounding, its temperature increases by

- (a)  $\frac{(\gamma - 1)}{2(\gamma + 1)R} Mv^2 K$       (b)  $\frac{(\gamma - 1)}{2\gamma} Mv^2 K$       (c)  $\frac{\gamma Mv^2}{2R} K$       (d)  $\frac{(\gamma - 1)}{2R} Mv^2 K$

Q.10 A point mass oscillates along the  $x$ -axis according to the law  $x = x_0 \cos\left(\omega t - \frac{\pi}{4}\right)$ . If

acceleration of the particle is written  $a = A(\omega t + \delta)$ , then

- (a)  $A = x_0 \omega^2, \delta = \frac{\pi}{4}$       (b)  $A = x_0 \omega^2, \delta = -\frac{\pi}{4}$   
 (c)  $A = x_0 \omega^2, \delta = \frac{3\pi}{4}$       (d)  $A = x_0 \omega^2, \delta = -\frac{\pi}{4}$

Q.11 There is destructive interference between the two waves of wavelength  $\lambda$  coming from two different paths at a point. To get maximum sound or constructive interference at that point, the path of one wave is to be increased by

- (a)  $\lambda / 4$       (b)  $\lambda / 2$       (c)  $3\lambda / 4$       (d)  $\lambda$

Q.12 Two point charges  $-Q$  and  $2Q$  are separated by a distance  $R$ . The neutral point will be obtained at,

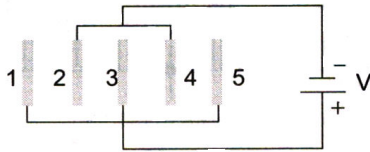
- (a) A distance of  $\frac{R}{(\sqrt{2} - 1)}$  from  $-Q$  charge and lies between the charges.  
 (b) A distance of  $\frac{R}{(\sqrt{2} - 1)}$  from  $-Q$  charge on the left side of it.  
 (c) A distance of  $\frac{R}{(\sqrt{2} - 1)}$  from  $2Q$  charge on the right side of it  
 (d) A point on the line which passes perpendicularly through the centre of the line joining  $-Q$  and  $2Q$  charges.

Q.13 The potential at point  $x$  (measured in  $\mu\text{m}$ ) due to some charges situated on the  $x$ -axis is given by  $V(x) = 200 / (x^2 - 4)$  Volt. The electric field  $E$  at  $x = 4 \mu\text{m}$  is given by

- (a)  $5 / 3 V / \mu\text{m}$  and in the positive  $x$ -direction

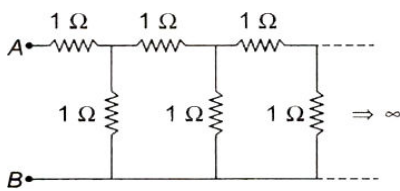
- (b)  $10/9V/\mu\text{m}$  and in the negative x-direction
- (c)  $10/9V/\mu\text{m}$  and in the positive x-direction
- (d)  $5/3V/\mu\text{m}$  and in the negative direction.

Q.14 Five similar condenser plates, each of area  $A$  are placed at equal distance  $d$  apart and are connected to a source of emf  $E$  as shown in figure. The charge on the plates 1 and 4 will be



- (a)  $\frac{\epsilon_0 A}{d}, \frac{-2\epsilon_0 A}{d}$
- (b)  $\frac{\epsilon_0 AV}{d}, \frac{-2\epsilon_0 AV}{d}$
- (c)  $\frac{\epsilon_0 AV}{d}, \frac{-3\epsilon_0 AV}{d}$
- (d)  $\frac{\epsilon_0 AV}{d}, \frac{-4\epsilon_0 AV}{d}$

Q.15 The equivalent resistance between points  $A$  and  $B$  of an infinite network of resistance, each of  $1\Omega$  connected as shown in figure is



- (a) Infinite
- (b)  $2\Omega$
- (c)  $\frac{1+\sqrt{5}}{2}\Omega$
- (d) Zero

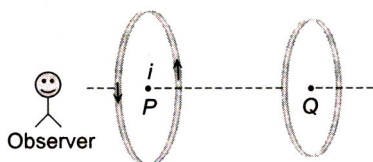
Q.16 A particle of charge  $q$  and mass  $m$  starts moving from the origin under the action of an electric field  $\vec{E} = E_0 \hat{i}$  and  $\vec{B} = B_0 \hat{i}$  with a velocity  $\vec{v} = v_0 \hat{j}$ . The speed of the particle will become  $2v_0$  after a time

- (a)  $t = \frac{2mv_0}{qE}$
- (b)  $t = \frac{2Bq}{mv_0}$
- (c)  $t = \frac{\sqrt{3}Bq}{mv_0}$
- (d)  $t = \frac{\sqrt{3}mv_0}{qE}$

Q.17 The plane of dip circle is set in the geographic meridian and the apparent dip is  $\theta_1$ . It is then set in a vertical plane perpendicular to the geographic meridian. Now the apparent dip is  $\theta_2$ . The angle of declination  $\alpha$  at that place is

- (a)  $\tan \alpha = \sqrt{\tan \theta_1 \tan \theta_2}$
- (b)  $\tan \alpha = \sqrt{(\tan \theta_1)^2 + (\tan \theta_2)^2}$
- (c)  $\tan \alpha = \frac{\tan \theta_1}{\tan \theta_2}$
- (d)  $\tan \alpha = \frac{\tan \theta_2}{\tan \theta_1}$

Q.18 Two coils  $P$  and  $Q$  are lying a little distance apart coaxially. If an anticlockwise current  $i$  is suddenly set up in the coil  $P$  then the direction of current induced in coil  $Q$  will be

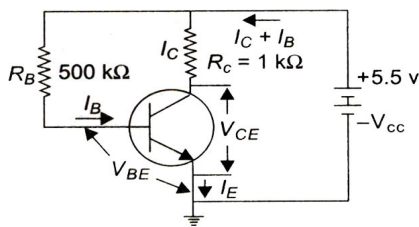


- (a) Clockwise
- (b) Towards north
- (c) Towards south
- (d) Anticlockwise

Q.19 A transformer is used to light  $140\text{ W}, 24\text{ V}$  lamp from  $240\text{ V}$  ac mains. If the current in the mains is  $0.7\text{ A}$ , then the efficiency of transformer is

- (a) 63.8%                      (b) 84%                      (c) 83.3%                      (d) 48%

- Q.20 A parallel plate capacitor consists of two circular plates each of radius 2 cm, separated by a distance of 0.1 mm. If voltage across the plates is varying at the rate of  $5 \times 10^{13}$  V/s, Then the value of displacement current is  
 (a) 5.50 A                      (b)  $5.56 \times 10^2$  A                      (c)  $5.56 \times 10^3$  A                      (d)  $2.28 \times 10^4$  A
- Q.21 A 2-V battery, a  $-15\Omega$  resistor, and a potentiometer of 100 cm length, all are connected in series. If the resistance of potentiometer wire is  $5-\Omega$ , then the potential gradient of the potentiometer wire is \_\_\_\_\_?
- Q.22 A double slit arrangement produces interference fringes for sodium light ( $\lambda = 589$  nm) that have an angular separation of  $3.50 \times 10^{-3}$  radian, For what wavelength would the angular separation be 10% greater?
- Q.23 In the circuit shown in the figure, the base current  $I_B$  is  $10 \mu\text{A}$  and the collector is 5.2 mA. The value of  $V_{BE}$  is \_\_\_\_\_?



- Q.24 An ice box used for keeping eatables has a total wall area of  $1 \text{ m}^2$  and a wall thickness of 5.0 cm. The thermal conductivity of the ice box is  $K = 0.01 \text{ J/m}^\circ\text{C}$ . It is filled with ice at  $0^\circ\text{C}$  along with eatables on a day when the temperature is  $30^\circ\text{C}$ . The latent heat of fusion of ice is  $334 \times 10^3 \text{ J/kg}$ . The amount of ice melted on one day is \_\_\_\_\_?  
 (1 day = 86,400 s)
- Q.25 A screw gauge gives the following reading when used to measure the diameter of a wire. Main scale reading: 0 mm Circular scale reading: 52 divisions Given that 1 mm on main scale corresponds to 100 divisions of the circular scale, the diameter of wire from the above data is \_\_\_\_\_?

## Part - B - CHEMISTRY

- Q.26 The oxidation number of sulphur in  $\text{Sg}$ ,  $\text{S}_2$ ,  $\text{F}_2$ ,  $\text{H}_2\text{S}$  respectively. are :  
 (a) 0, +1, and -2                      (b) +2, +1, and -2                      (c) 0, +1, and +2                      (d) -2, +1 and -2
- Q.27 Uncertainty in position is twice the uncertainty in momentum. Uncertainty in velocity is :  
 (a)  $\sqrt{\frac{h}{\pi}}$                       (b)  $\frac{1}{2m} \sqrt{\frac{h}{\pi}}$                       (c)  $\frac{1}{2m} \sqrt{h}$                       (d)  $\frac{h}{4\pi}$
- Q.28 The common features among the species  $\text{CN}^-$ ,  $\text{CO}$ , and  $\text{NO}^+$  are  
 (a) Bond order three and isoelectronic  
 (b) Bond order three and weak field ligands  
 (c) Bond order two and  $\pi$ -acceptors  
 (d) Isoelectronic and weak field ligands
- Q.29  $\text{N}_2 + 3\text{H}_2 \longrightarrow 2\text{NH}_3$ , 1 mol  $\text{N}_2$  and 4 mol  $\text{H}_2$  are taken in a 15-L flask at  $27^\circ\text{C}$ . After complete conversion of  $\text{N}_2$  into  $\text{NH}_3$ , 5 L of  $\text{H}_2\text{O}$  is added. Pressure set up in the flask is :

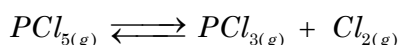
- (a)  $\frac{3 \times 0.0821 \times 300}{15}$  atm                      (b)  $\frac{2 \times 0.0821 \times 300}{10}$  atm  
 (c)  $\frac{1 \times 0.0821 \times 300}{15}$  atm                      (d)  $\frac{1 \times 0.0821 \times 300}{10}$  atm

Q.30 In harber's process of ammonia manufacture :  $N_{2(g)} + 3H_{2(g)} \rightarrow 2NH_{3(g)}$ ;  $H_{25^\circ C}^0 = -92.2 \text{ kJ}$

Molecule	$N_{2(g)}$	$H_{2(g)}$	
$NH_{3(g)}$			
Cp (J/K mol)	29.1	28.8	35.1

In Cp is independent of temperature, then reaction at  $100^\circ\text{C}$  as compared to the of  $25^\circ\text{C}$  will be

- (a) more endothermic                      (b) less endothermic  
 (c) more exothermic                      (d) less exothermic
- Q.31  $PCl_5$  dissociation in a closed container is given as :



If the total pressure at equilibrium of the reaction mixture is  $P$  and the degree of dissociation of  $PCl_5$  is  $\alpha$ , the partial pressure of  $PCl_3$  will be :

- (a)  $P \times \left[ \frac{\alpha}{\alpha+1} \right]$                       (b)  $P \times \left[ \frac{2\alpha}{1-\alpha} \right]$                       (c)  $P \times \left[ \frac{\alpha}{\alpha-1} \right]$                       (d)  $P \times \left[ \frac{\alpha}{1-\alpha} \right]$

Q.32 For a sparingly soluble salt  $A_p B_q$ , the relationship of its solubility product ( $L_s$ ) with its solubility (S) is :

- (a)  $L_s = S^{p+q} \cdot p^p \cdot q^q$                       (b)  $L_s = S^{p+q} \cdot p^q \cdot q^p$                       (c)  $L_s = S^{pq} \cdot p^p \cdot q^q$                       (d)  $L_s = S^{pq} \cdot (p \cdot q)^{p+q}$

Q.33 A compound has the empirical formula  $C_{10}H_8Fe$ . A solution of 0.26 g of the compound in 11.2 g of benzene ( $C_6H_6$ ) boils at  $80.26^\circ\text{C}$ . The boiling point of benzene is  $80.10^\circ\text{C}$  and  $K_b$  is  $2.53^\circ\text{C/molal}$ . What is the molecular formula of the compound ?

- (a)  $C_{30}H_{24}Fe_3$                       (b)  $C_{10}H_8Fe$                       (c)  $C_5H_4Fe$                       (d)  $C_{20}H_{16}Fe_2$

Q.34 For the cell  $Ti | Ti || Cu^{2+} | Cu$ ,  $E_{cell}$  at  $25^\circ\text{C}$  is 0.83 V. The EMF of the cell can be increased by :

- (a) increasing  $[Cu^{2+}]$                       (b) increasing  $[Ti^+]$   
 (c) decreasing  $[Cu^{2+}]$                       (d) increasing temperature to  $35^\circ\text{C}$

Q.35 Under the influence of an electric field, the particle in a sol migrate towards cathode. The coagulation of the same sol is studied using  $NaCl$ ,  $Na_2SO_4$  and  $Na_3SO_4$  solution. Their coagulating values will be maximum for :

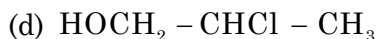
- (a)  $NaCl$                       (b)  $Na_2SO_4$                       (c)  $Na_3PO_4$                       (d) Same for all

Q.36 An organic compound (A) has the molecular formula  $C_3H_6O$ . It undergoes iodoform test. When saturated with dil.  $HCl$ , it gives (B) of molecular formula  $C_9H_{14}O$ . A and B respectively are :

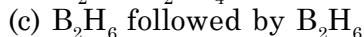
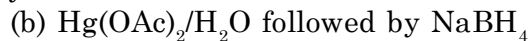
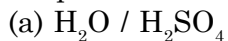
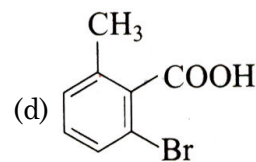
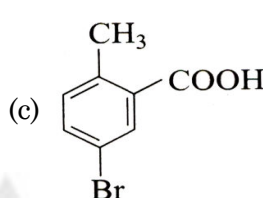
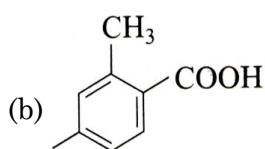
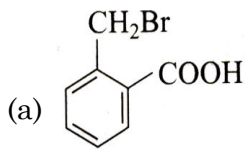
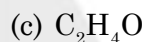
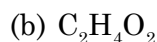
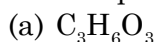
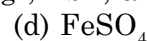
- (a) propanal and mesitylene  
 (b) propanone and mesityl oxide  
 (c) propanone and 2,6-dimethyl-2,5-heptadien-4-one  
 (d) propanone and mesitylene oxide

Q.37 Among the following which one can have a meso form ?

- (a)  $CH_3 - CHOH - CH(Cl) - C_2H_5$   
 (b)  $CH_3 - CHOH - CHOH - CH_3$



Q.38 Propan-1-ol can be prepared from propane by alcohol :

Q.39 o-Toluic acid on reaction with  $\text{Br}_2/\text{Fe}$  gives :Q.40 Empirical formula of a compound is  $\text{CH}_2\text{O}$  and its vapor density is 30. Molecular formula of the compound is :Q.41 A colorless water-soluble solid X on heating gives equimolar quantities of Y and Z. Y gives dense white fumes with  $\text{HCl}$  and Z does so with  $\text{NH}_3$ . Y gives brown precipitate with Nessler's reagent and Z gives white precipitate with nitrates of  $\text{Ag}^+$ ,  $\text{Pb}^{2+}$ , and  $\text{Hg}^+$ , X is

Q.42 Setting of plaster of Paris is :

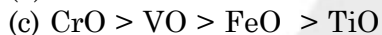
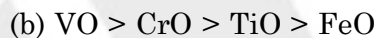
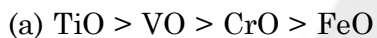
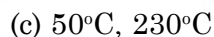
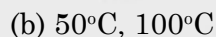
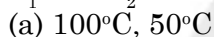
(a) oxidation with atmospheric oxygen

(b) combination with atmospheric  $\text{CO}_2$ 

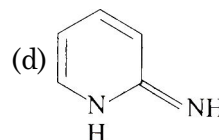
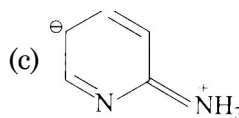
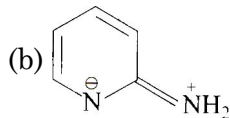
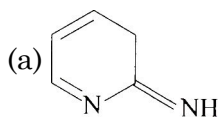
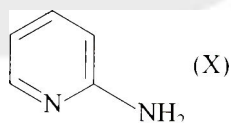
(c) dehydration

(d) hydration to yield another hydrate

Q.43 The basic character of the transition metal monoxides follows the order :

Q.44 Formation of  $\text{Ni}(\text{CO})_4$  and its subsequent decomposition into Ni and CO (recycled) make basis of Mond's process :  $\text{Ni} + 4\text{CO} \xrightarrow{T_1} \text{Ni}(\text{CO})_4 \xrightarrow{T_2} \text{Ni} + 4\text{CO}$  $T_1$  and  $T_2$  are

Q.45 The proper tautomeric structure for 2-aminopyridine (X) is :

Q.46  $x\text{A} + y\text{B} \rightarrow z\text{C}$ . If  $-\frac{d[\text{A}]}{dt} = -\frac{d[\text{B}]}{dt} = 1.5 \frac{d[\text{C}]}{dt}$ , then x, y, and z are :

Q.47 The density of a pure substance "A" whose atoms pack in cubic close pack arrangement is 1 g/cc. If B atoms can occupy tetrahedral void and if all the tetrahedral voids are occupied by B atom, what is the density of resulting solid in g/cc.

[Atomic mass A = 30 g/mol and atomic mass (B) = 50 g/mol]

- Q.48 What volume of liquid A has the same mass as  $80.0 \text{ cm}^3$  of liquid B ?
- Q.49 Oxidation states of vanadium in  
 $V \rightarrow V^{2+} + 2e$ ,  
 $V^{2+} \rightarrow V^{3+} + e$ ,  
 are 2 and 3 respectively. The oxidation states of vanadium in this following reaction  
 $V^{3+} + H_2O \rightarrow VO^{2+} + 2H^+ + e^-$  ?
- Q.50 A 25.0 mL sample of 0.1050 M  $H_2SO_4$  is titrated with NaOH solution of unknown concentration. The phenolphthalein indicator end point was reached when 17.23 mL of NaOH solution had been added. What is the concentration of the NaOH ?

## Part - C - MATHEMATICS

- Q.51 The 120 permutations of MAHES are arranged in dictionary order, as if each were an ordinary five-letter word. The last letter of the 86th word in the list is  
 (a) A (b) H (c) S (d) E
- Q.52  $\log_7 \log_7 \sqrt{7\sqrt{(7\sqrt{7})}}$  is equal to  
 (a)  $3 \log_2 7$  (b)  $3 \log_7 2$  (c)  $1 - 3 \log_7 2$  (d)  $1 - 3 \log_7 7$
- Q.53 The area of the quadrilateral  $ABCD$  whose vertices are respectively  $A(1, 1)$ ,  
 $B(7, -3)$ ,  $C(12, 2)$  and  $(7, 21)$  is  
 (a) 100 sq. units (b) 125 sq. units (c) 132 sq. units (d) none of these
- Q.54 If non-zero numbers  $a, b, c$  are in HP, then the straight line  $\frac{x}{a} + \frac{y}{b} + \frac{1}{c} = 0$  always passes through a fixed point. The point is  
 (a)  $(-1, -2)$  (b)  $(-1, 2)$  (c)  $\left(1, -\frac{1}{2}\right)$  (d)  $(1, -2)$
- Q.55 If a line is drawn through a fixed point  $P(\alpha, \beta)$  to cut the circle  $x^2 + y^2 = a^2$  at A and B, then  $PA \cdot PB =$   
 (a)  $\alpha^2 + \beta^2$  (b)  $\alpha^2 + \beta^2 - a^2$  (c)  $a^2$  (d)  $\alpha^2 + \beta^2 + a^2$
- Q.56 The curve described parametrically by  $x = t^2 + r + 1$ ,  $y = t^2 - t + 1$  represents  
 (a) a pair of straight lines (b) an ellipse  
 (c) a parabola (d) a hyperbola
- Q.57 If any tangent to the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  intercept equal lengths  $\ell$  on the axes, then  $\ell =$   
 (a)  $a^2 + b^2$  (b)  $\sqrt{a^2 + b^2}$  (c)  $(a^2 + b^2)^2$  (d) none of these
- Q.58 Two straight lines pass through the fixed points  $(\pm a, 0)$  and have slopes whose products is  $p > 0$ . Then the locus of the points of intersection of the lines is  
 (a) ellipse (b) hyperbola (c) parabola (d) circle
- Q.59 If  $f(x + 2y, x - 2y) = xy$ , then  $f(x, y)$  equal



- (a)  $(x^2 - y^2) / 8$       (b)  $(x^2 - y^2) / 4$       (c)  $(x^2 + y^2) / 4$       (d)  $(x^2 - y^2) / 2$

Q.60 The inverse of the function  $f(x) = \frac{e^x - e^{-x}}{e^x + e^{-x}} + 2$  is given by

- (a)  $\log_e \left( \frac{x-2}{x-1} \right)^{\frac{1}{2}}$       (b)  $\log_e \left( \frac{x-1}{3-x} \right)^{\frac{1}{2}}$       (c)  $\log_e \left( \frac{x}{2-x} \right)^{\frac{1}{2}}$       (d)  $\log_e \left( \frac{x-1}{x+1} \right)^{\frac{1}{2}}$

Q.61 If  $f(x) = \begin{cases} \sin x, & x \neq n\pi, n \in \mathbb{Z} \\ 0, & \text{otherwise} \end{cases}$  and  $g(x) = \begin{cases} x^2 + 1, & x \neq 0, 2 \\ 4, & x = 0 \\ 5, & x = 2 \end{cases}$  then  $\lim_{x \rightarrow 0} g\{f(x)\} =$

- (a) 1      (b) 0      (c)  $\frac{1}{2}$       (d)  $\frac{1}{4}$

Q.62 The expression  $y^2 \frac{d^2 y}{dx^2}$  on the ellipse  $3x^2 + 4y^2 = 12$  is equal to

- (a)  $\frac{9}{4}$       (b)  $-\frac{9}{4}$       (c)  $\frac{4}{9}$       (d)  $-\frac{4}{9}$

Q.63 The lateral edge of a regular rectangular pyramid is "a" cm long. The lateral edge makes an angle  $\alpha$  with the plane of the base. The value of  $\alpha$  for which the volume of the pyramid is greatest is

- (a)  $\frac{\pi}{4}$       (b)  $\sin^{-1} \sqrt{\frac{2}{3}}$       (c)  $\cot^{-1} \sqrt{2}$       (d)  $\frac{\pi}{3}$

Q.64  $\int \frac{2x}{(1-x^2)\sqrt{x^4-1}} dx$  is equal to

- (a)  $\sqrt{\frac{x^2+1}{x^2-1}} + c$       (b)  $\sqrt{\frac{x^2-1}{x^2+1}} + c$       (c)  $\sqrt{x^4-1} + c$       (d) none of these

Q.65 The area of the closed figure bounded by  $x = -1$  and  $x = 2$  and  $y = \begin{cases} -x^2 + 2, & x \leq 1 \\ 2x - 1, & x > 1 \end{cases}$  and the abscissa axis is

- (a)  $\frac{16}{3}$  sq units      (b)  $\frac{10}{3}$  sq units      (c)  $\frac{13}{3}$  sq units      (d)  $\frac{7}{3}$  sq units

Q.66 An object falling from rest in the air is subjected not only to the gravitational force but also to the air resistance. Assume that the air resistance is proportional to the velocity with constant of proportionality as  $k > 0$ , and acts in a direction opposite to motion ( $g = 9.8 \text{ m/sec}^2$ ). Then velocity cannot exceed

- (a)  $9.8/k$  m/sec      (b)  $9.8/k$  m/sec      (c)  $\frac{k}{9.8}$  m/sec      (d) none of these

Q.67 The variable "x" satisfying the equation  $|\sin x \times \cos x| + \sqrt{2 + \tan^2 x + \cot^2 x} = \sqrt{3}$ , belongs to the interval

- (a)  $\left[0, \frac{\pi}{3}\right]$       (b)  $\left(\frac{\pi}{3}, \frac{\pi}{2}\right)$       (c)  $\left[\frac{3\pi}{4}, \pi\right)$       (d) non-existent

Q.68 The equation  $2\cos^2 \frac{x}{2} \sin^2 x = x^2 + x^{-2}$ ;  $0 < x \leq \frac{\pi}{2}$  has

- (a) no real solution      (b) one real solution  
(c) more than one solution      (d) none of these

Q.69 Which of the following is the solution set of the equation  $2\cos^{-1} x = \cot^{-1} \left( \frac{2x^2 - 1}{2x\sqrt{1-x^2}} \right)$ ?

- (a) (0, 1)      (b) (-1, 1) - {0}      (c) (-1, 0)      (d) [-1, 1]

Q.70 If  $x, y, z$  are drawn perpendicular to  $a, b,$  and  $c$ , then the value of  $\frac{bx}{c} + \frac{cy}{a} + \frac{az}{b}$  will be

- (a)  $\frac{a^2 + b^2 + c^2}{2R}$       (b)  $\frac{a^2 + b^2 + c^2}{R}$       (c)  $\frac{a^2 + b^2 + c^2}{4R}$       (d)  $\frac{2(a^2 + b^2 + c^2)}{2R}$

Q.71 The coefficient of  $x^4$  in the expansion of  $(1 + x + x^2 + x^3)^{11}$  is \_\_\_\_\_?

Q.72 Solve :  $\int_0^{\frac{\pi}{2}} \frac{dx}{1 + \cos x} =$

Q.73 If  $\frac{dy}{dx} = y + 3 > 0$  and  $y(0) = 2$ , then  $y(\ln 2)$  is equal to ?

Q.74 If  $A = \begin{vmatrix} 1 & -1 & 1 \\ 1 & 2 & 0 \\ 1 & 3 & 0 \end{vmatrix}$  then the value of  $|\text{adj } A|$  is equal to ?

Q.75 The value of  $\int_{-1}^1 |x+1| dx$  is \_\_\_\_\_?

\*\*\*\*\*

---

## ROUGH WORK

---

## ROUGH WORK