

JEE MATHEMATICS

Topic: Indefinite Integration

Q.1 $\int \frac{x^5}{1+x^{12}} dx$ is equal to-

(A) $\tan^{-1}x^6 + c$ (B) $2 \tan^{-1}x^6 + c$

(C) $\frac{1}{6} \tan^{-1}x^6 + c$ (D) None of these

Q.2 $\int \sin \sqrt{x} dx$ is equal to-

(A) $2 (\sin \sqrt{x} - \cos \sqrt{x}) + c$

(B) $2 (\sin \sqrt{x} + \cos \sqrt{x}) + c$

(C) $2 (\sin \sqrt{x} - \sqrt{x} \cos \sqrt{x}) + c$

(D) $2 (\sin \sqrt{x} + \sqrt{x} \cos \sqrt{x}) + c$

Q.3 $\int \frac{dx}{x+x \log x}$ is equal to-

(A) $\log x + \log (\log x) + c$

(B) $\log \log (1+ \log x) + c$

(C) $\log (1+ \log x) + c$

(D) None of these

Q.4 $\int e^{x/2} \sin \left(\frac{x}{2} + \frac{\pi}{4} \right) dx$ is equal to-

(A) $e^{x/2} \sin x/2 + c$

(B) $e^{x/2} \cos x/2 + c$

(C) $\sqrt{2} e^{x/2} \sin x/2 + c$

(D) $\sqrt{2} e^{x/2} \cos x/2 + c$

Q.5 $\int \{\sin(\log x) + \cos(\log x)\} dx$ is equal to-

(A) $\sin(\log x) + c$

(B) $\cos(\log x) + c$

(C) $x \sin(\log x) + c$

(D) $x \cos(\log x) + c$

Q.6 $\int \log_{10} x dx$ is equal to-

(A) $\log_{10} x + c$

(B) $x \log_{10} x + c$

(C) $x(\log_{10} x + \log_{10} e) + c$

(D) $x(\log_{10} x - \log_{10} e) + c$

Q.7 $\int [(\log 2x)/x] dx$ equals-

(A) $x \log 2x + c$

(B) $(\log x \log 2x)/2 + c$

(C) $(\log x \log 4x)/2 + c$

(D) None of these

Q.8 $\int \sqrt{\frac{x}{a^3 - x^3}} dx$ is equal to-

(A) $\sin^{-1} \left(\frac{x}{a} \right)^{3/2} + c$

(B) $\frac{2}{3} \sin^{-1} \left(\frac{x}{a} \right)^{3/2} + c$

(C) $\frac{3}{2} \sin^{-1} \left(\frac{x}{a} \right)^{3/2} + c$

(D) $\frac{3}{2} \sin^{-1} \left(\frac{x}{a} \right)^{2/3} + c$

Q.9 $\int \frac{dx}{\sin(x-a)\cos(x-b)}$ is equal to-

(A) $\cos(a-b) \log \frac{\sin(x-a)}{\cos(x-b)} + c$

(B) $\sec(a-b) \log \frac{\sin(x-a)}{\cos(x-b)} + c$

(C) $\sin(a-b) \log \frac{\cos(x-a)}{\sin(x-b)} + c$

(D) $\operatorname{cosec}(a-b) \log \frac{\cos(x-a)}{\sin(x-b)} + c$

Q.10 $\int x \cos^2 x \, dx$ is equal to-

(A) $\frac{x^2}{4} - \frac{1}{4} x \sin 2x - \frac{1}{8} \cos 2x + c$

(B) $\frac{x^2}{4} - \frac{1}{4} x \sin 2x + \frac{1}{8} \cos 2x + c$

(C) $\frac{x^2}{4} + \frac{1}{4} x \sin 2x - \frac{1}{8} \cos 2x + c$

(D) $\frac{x^2}{4} + \frac{1}{4} x \sin 2x + \frac{1}{8} \cos 2x + c$

Q.11 $\int x^{51} (\tan^{-1} x + \cot^{-1} x) \, dx$ is equal to-

(A) $\frac{x^{52}}{52} (\tan^{-1} x + \cot^{-1} x) + c$

(B) $\frac{x^{52}}{52} (\tan^{-1} x - \cot^{-1} x) + c$

(C) $\frac{x^{52}}{52} + \frac{\pi}{2} + c$

(D) $-\frac{\pi x^{52}}{104} + \frac{\pi}{2} + c$

Q.12 $\int \frac{\sin^8 x - \cos^8 x}{1 - 2\sin^2 x \cos^2 x} dx$ is equal to-

(A) $\sin 2x + c$ (B) $-\frac{1}{2} \sin 2x + c$

(C) $\frac{1}{2} \sin 2x + c$ (D) $-\sin 2x + c$

Q.13 If $\int f(x) dx = F(x)$, then $\int x^3 f(x^2) dx$ equals

(A) $\frac{1}{2} [x^2 F(x^2) - \int F(x^2) dx^2]$

(B) $\frac{1}{2} [x^2 F(x^2) - \int F(x^2) dx]$

(C) $\frac{1}{2} [x^2 F(x) - \frac{1}{2} \int F(x^2) dx]$

(D) none of these

Q.14 If $I = \int e^x \sin 2x dx$, then for what value of k, $kI = e^x (\sin 2x - 2 \cos 2x) + \text{constant}$ -

(A) 1 (B) 3 (C) 5 (D) 7

Q.15 $\int \frac{\cos 4x + 1}{\cot x - \tan x} dx$ equals-

(A) $-\frac{1}{2} \cos 4x + c$ (B) $-\frac{1}{2} \cos 4x + c$

(C) $-\frac{1}{8} \cos 4x + c$ (D) None of these

Q.16 $\int \frac{x^2 + 1}{(x+1)^2} e^x dx$ equal to-

(A) $\frac{x-1}{x+1} e^x + c$ (B) $\frac{x+1}{x-1} e^x + c$

(C) $\frac{x}{(x+1)^2} e^x + c$ (D) $\frac{x}{x+1} e^x + c$

Q.17 $\int \frac{3 \tan \frac{x}{3} - \tan^3 \frac{x}{3}}{1 - 3 \tan^2 \frac{x}{3}} dx$ is equal to-

- (A) $-\log |\sec x| + c$
- (B) $-\log |(\cos x)| + c$
- (C) $\sec^2 x + c$
- (D) $\log |\tan x| + c$

Q.18 $\int \cos^3 x e^{\log(\sin x)} dx$ is equal to-

- (A) $\frac{1}{4} e^{\sin x} + c$
- (B) $-\frac{1}{4} \sin^4 x + c$
- (C) $-\frac{1}{4} \cos^4 x + c$
- (D) None of these

Q.19 $\int e^{\tan^{-1} x} \left(\frac{1+x+x^2}{1+x^2} \right) dx$ is equal to-

- (A) $x e^{\tan^{-1} x} + c$
- (B) $x^2 e^{\tan^{-1} x}$
- (C) $\frac{1}{x} e^{\tan^{-1} x} + c$
- (D) None of these

Q.20 $\int \sqrt{\frac{\cos x - \cos^3 x}{1 - \cos^3 x}} dx$ is equal to-

- (A) $\frac{2}{3} \sin^{-1}(\cos^3/2 x) + c$
- (B) $\frac{3}{2} \sin^{-1}(\cos^3/2 x) + c$
- (C) $\frac{2}{3} \cos^{-1}(\cos^3/2 x) + c$
- (D) None of these

Q.21 If $\int \frac{dx}{x\sqrt{1-x^3}} = a \log \left[\frac{\sqrt{1-x^3}-1}{\sqrt{1-x^3}+1} \right] + b$, then-

(A) $a = \frac{1}{3}$

(B) $a = \frac{2}{3}$

(C) $a = -\frac{1}{3}$

(D) $a = -\frac{2}{3}$

Q.22 $\int \frac{x \tan^{-1} x}{(1+x^2)^{3/2}} dx$ equals to-

(A) $\frac{x \tan^{-1} x}{\sqrt{1+x^2}} + c$

(B) $\frac{x - \tan^{-1} x}{\sqrt{1+x^2}} + c$

(C) $\frac{\tan^{-1} x - x}{\sqrt{1+x^2}} + c$

(D) None of these

Q.23 $\int \frac{3 \cos x + 2 \sin x}{4 \sin x + 5 \cos x} dx$ is equal to-

(A) $\frac{23}{41} x + \frac{2}{41} \log (4 \sin x + 5 \cos x) + c$

(B) $\frac{23}{41} x - \frac{2}{41} \log (4 \sin x + 5 \cos x) + c$

(C) $\frac{23}{41} x - \frac{2}{41} \log (4 \sin x - 5 \cos x) + c$

(D) None of these

Q.24 $\int \frac{x^2 + 1}{x(x^2 - 1)} dx$ is equal to-

(A) $\log\left(\frac{x^2 - 1}{x}\right) + c$

(B) $-\log\left(\frac{x^2 - 1}{x}\right) + c$

(C) $\log\left(\frac{x}{x^2 + 1}\right) + c$

(D) $-\log\left(\frac{x}{x^2 + 1}\right) + c$

Q.25 $\int x^n \log x dx$ equals-

(A) $\frac{x^{n+1}}{n+1} \left\{ \log x + \frac{1}{n+1} \right\} + c$

(B) $\frac{x^{n+1}}{n+1} \left\{ \log x + \frac{2}{n+1} \right\}$

(C) $\frac{x^{n+1}}{n+1} \left\{ 2 \log x - \frac{1}{n+1} \right\} + c$

(D) $\frac{x^{n+1}}{n+1} \left\{ \log x - \frac{1}{n+1} \right\} + c$

Q.26 $\int \tan^{-1}(\sec x + \tan x) dx$ equals-

(A) $\frac{x}{2} + c$

(B) $\frac{\sec x}{\sec x + \tan x} + c$

(C) $\frac{x}{4}(\pi + x) + c$

(D) None of these

Q.27 $\int \frac{4x - 7}{x^2 + x - 2} dx$ equals-

(A) $2 \log(x^2 + x - 2) - 3 \log\left(\frac{x-1}{x+2}\right) + c$

(B) $2 \log(x^2 + x - 2) + 3 \log\left(\frac{x-1}{x+2}\right) + c$

(C) $3 \log(x^2 + x - 2) + 2 \log\left(\frac{x-1}{x+2}\right) + c$

(D) None of these

Q.28 $\int \cos^2(ax + b) \sin(ax + b) dx$ equals-

(A) $-\frac{\cos^3(ax + b)}{3a} + c$

(B) $\frac{\cos^3(ax + b)}{3a} + c$

(C) $\frac{\sin^3(ax + b)}{3a} + c$

(D) $-\frac{\sin^3(ax + b)}{3a} + c$

Q.29 $\int \sqrt{1 + \sec x} dx$ equals-

(A) $2 \sin^{-1}(\sqrt{2} \sin x/2) + c$

(B) $-2 \sin^{-1}(\sqrt{2} \sin x/2) + c$

(C) $2 \log \left| \sqrt{2} \sin \frac{x}{2} + \sqrt{2 \sin^2 \frac{x}{2} - 1} \right|$

(D) None of these

Q.30 $\int \frac{\sin x}{\sin 3x} dx$ is equal to-

(A) $\frac{1}{2\sqrt{3}} \log \left(\frac{\sqrt{3} + \tan x}{\sqrt{3} - \tan x} \right) + c$

(B) $\frac{1}{2\sqrt{3}} \log \left(\frac{\sqrt{3} - \tan x}{\sqrt{3} + \tan x} \right) + c$

(C) $\frac{1}{\sqrt{3}} \log \left(\frac{\sqrt{3} + \tan x}{\sqrt{3} - \tan x} \right) + c$

(D) None of these

ANSWER KEY

Que.	1	2	3	4	5	6	7	8	9	10
Ans.	C	C	C	C	C	D	C	B	B	D
Que.	11	12	13	14	15	16	17	18	19	20
Ans.	A	B	A	C	C	A	B	C	A	C
Que.	21	22	23	24	25	26	27	28	29	30
Ans.	A	B	A	A	D	C	A	A	A	A

