

JEE MATHEMATICS

Topic: Hyperbola

Q.1 The vertices of a hyperbola are at (0, 0) and (10, 0) and one of its foci is at (18, 0). The equation of the hyperbola is -

(A) $\frac{x^2}{25} - \frac{y^2}{144} = 1$ (B) $\frac{(x-5)^2}{25} - \frac{y^2}{144} = 1$

(C) $\frac{x^2}{25} - \frac{(y-5)^2}{144} = 1$ (D) $\frac{(x-5)^2}{25} - \frac{(y-5)^2}{144} = 1$

Q.2 If the latus rectum of an hyperbola be 8 and eccentricity be $\frac{3}{\sqrt{5}}$, then the equation of the hyperbola is-

(A) $4x^2 - 5y^2 = 100$ (B) $5x^2 - 4y^2 = 100$

(C) $4x^2 + 5y^2 = 100$ (D) $5x^2 + 4y^2 = 100$

Q.3 The foci of the hyperbola

$9x^2 - 16y^2 + 18x + 32y - 151 = 0$ are-

(A) (2, 3), (5, 7) (B) (4, 1), (-6, 1)

(C) (0, 0), (5, 3) (D) None of these

Q.4 The foci of the hyperbola $4x^2 - 9y^2 - 36 = 0$ are-

(A) $[\pm\sqrt{11}, 0]$ (B) $[\pm\sqrt{12}, 0]$

(C) $[\pm\sqrt{13}, 0]$ (D) $[0, \pm\sqrt{12}]$

Q.5 Foci of the hyperbola $\frac{x^2}{16} - \frac{(y-2)^2}{9} = 1$ are

- (A) (5, 2); (-5, 2) (B) (5, 2); (5, -2)
(C) (5, 2); (-5, -2) (D) None of these

Q.6 The eccentricity of a hyperbola $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$ passing through the points (3, 0), ($3\sqrt{2}$, 2) will be-

- (A) $\sqrt{13}$ (B) $\frac{\sqrt{13}}{3}$
(C) $\frac{\sqrt{13}}{4}$ (D) $\frac{\sqrt{13}}{2}$

Q.7 Equation of the hyperbola with eccentricity $3/2$ and foci at $(\pm 2, 0)$ is-

- (A) $\frac{x^2}{4} - \frac{y^2}{5} = \frac{4}{9}$
(B) $\frac{x^2}{9} - \frac{y^2}{9} = \frac{4}{9}$
(C) $\frac{x^2}{4} - \frac{y^2}{9} = 1$
(D) None of these

Q.8 If the centre, vertex and focus of a hyperbola be (0, 0), (4, 0) and (6, 0) respectively, then the equation of the hyperbola is-

- (A) $4x^2 - 5y^2 = 8$ (B) $4x^2 - 5y^2 = 80$
(C) $5x^2 - 4y^2 = 80$ (D) $5x^2 - 4y^2 = 8$

Q.9 The eccentricity of the hyperbola can never be equal to-

- (A) $\sqrt{\frac{9}{5}}$ (B) $2\sqrt{\frac{1}{9}}$
(C) $3\sqrt{\frac{1}{8}}$ (D) $\sqrt{2}$

- Q.10** The eccentricity of the hyperbola whose latus rectum is 8 and conjugate axis is equal to half the distance between the foci is-
- (A) $\frac{4}{3}$ (B) $\frac{4}{\sqrt{3}}$
- (C) $\frac{2}{\sqrt{3}}$ (D) None of these
- Q.11** If the length of the transverse and conjugate axes of a hyperbola be 8 and 6 respectively, then the difference of focal distances of any point of the hyperbola will be-
- (A) 8 (B) 6
- (C) 14 (D) 2
- Q.12** If m is a variable, the locus of the point of intersection of the lines $\frac{x}{3} - \frac{y}{2} = m$ and $\frac{x}{3} + \frac{y}{2} = \frac{1}{m}$ is a/ an-
- (A) parabola (B) ellipse
- (C) hyperbola (D) None of these
- Q.13** The equation of the hyperbola whose foci are $(6, 5)$, $(-4, 5)$ and eccentricity $5/4$ is-
- (A) $\frac{(x-1)^2}{16} - \frac{(y-5)^2}{9} = 1$ (B) $\frac{x^2}{16} - \frac{y^2}{9} = 1$
- (C) $\frac{(x-1)^2}{9} - \frac{(y-5)^2}{16} = 1$ (D) None of these
- Q.14** The equation $\frac{x^2}{12-\lambda} + \frac{y^2}{8-\lambda} = 1$ represents
- (A) a hyperbola if $\lambda < 8$
- (B) an ellipse if $\lambda > 8$
- (C) a hyperbola if $8 < \lambda < 12$
- (D) None of these

- Q.15** The equation $ax^2 + 2hxy + by^2 + 2gx + 2fy + c = 0$ represents a rectangular hyperbola if-
- (A) $\Delta \neq 0, h^2 > ab, a + b = 0$
 (B) $\Delta \neq 0, h^2 < ab, a + b = 0$
 (C) $\Delta \neq 0, h^2 = ab, a + b = 0$
 (D) None of these
- Q.16** The equation $\frac{x^2}{1-k} - \frac{y^2}{1+k} = 1, k > 1$ represents-
- (A) circle (B) ellipse
 (C) hyperbola (D) None of these
- Q.17** If e and e' be the eccentricities of two conics S and S' such that $e^2 + e'^2 = 3$, then both S and S' are-
- (A) ellipse (B) parabolas
 (C) hyperbolas (D) None of these
- Q.18** A point moves in a plane so that its distances PA and PB from two fixed points A and B in the plane satisfy the relation $|PA - PB| = k (k \neq 0)$, then the locus of P is-
- (A) a parabola (B) an ellipse
 (C) a hyperbola (D) a branch of a hyperbola
- Q.19** The equation of the conic with focus at $(1, -1)$, directrix along $x - y + 1 = 0$ and with eccentricity $\sqrt{2}$ is-
- (A) $x^2 - y^2 = 1$ (B) $xy = 1$
 (C) $2xy - 4x + 4y + 1 = 0$ (D) $2xy + 4x - 4y - 1 = 0$

Q.20 The length of the latus rectum of the hyperbola $\frac{x^2}{a^2} - \frac{y^2}{b^2} = -1$ is-

(A) $\frac{2a^2}{b}$ (B) $\frac{2b^2}{a}$

(C) $\frac{b^2}{a}$ (D) $\frac{a^2}{b}$

Q.21 The equation $16x^2 - 3y^2 - 32x + 12y - 44 = 0$ represents a hyperbola-

(A) the length of whose transverse axis is $4\sqrt{3}$

(B) the length of whose conjugate axis is 4

(C) whose centre is $(-1, 2)$

(D) whose eccentricity is $\sqrt{\frac{19}{3}}$

Q.22 The length of the transverse axis of a hyperbola is 7 and it passes through the point $(5, -2)$. The equation of the hyperbola is-

(A) $\frac{4}{49}x^2 - \frac{196}{51}y^2 = 1$ (B) $\frac{49}{4}x^2 - \frac{51}{196}y^2 = 1$

(C) $\frac{4}{49}x^2 - \frac{51}{196}y^2 = 1$ (D) none of these

Q.23 The latus rectum of a hyperbola $\frac{x^2}{16} - \frac{y^2}{p} = 1$ is $4\frac{1}{2}$. Its eccentricity $e =$

(A) $4/5$ (B) $5/4$

(C) $3/4$ (D) $4/3$

Q.24 Consider the set of hyperbola $xy = k$, $k \in \mathbb{R}$. Let e_1 be the eccentricity when $k = 4$ and e_2 be the eccentricity when $k = 9$. Then $e_1^2 + e_2^2 =$

(A) 2 (B) 3

(C) 4 (D) 1

Q.25 The eccentricity of the hyperbola $-\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ is given by -

(A) $e = +\sqrt{\frac{a^2+b^2}{a^2}}$ (B) $e = +\sqrt{\frac{a^2-b^2}{a^2}}$

(C) $e = +\sqrt{\frac{b^2-a^2}{a^2}}$ (D) $e = +\sqrt{\frac{a^2+b^2}{b^2}}$

Q.26 If e and e' be the eccentricities of a hyperbola and its conjugate, then $\frac{1}{e^2} + \frac{1}{e'^2} =$

- (A) 0 (B) 1
(C) 2 (D) None of these

Q.27 The equation of a tangent parallel to $y = x$ drawn to $\frac{x^2}{3} - \frac{y^2}{2} = 1$ is-

- (A) $x - y + 1 = 0$ (B) $x - y + 2 = 0$
(C) $x + y - 1 = 0$ (D) $x - y + 2 = 0$

Q.28 The line $lx + my + n = 0$ will be a tangent to the hyperbola $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$, if -

- (A) $a^2l^2 + b^2m^2 = n^2$ (B) $a^2l^2 - b^2m^2 = n^2$
(C) $am^2 - b^2n^2 = a^2l^2$ (D) None of these

Q.29 The equation of tangents to the hyperbola $x^2 - 4y^2 = 36$ which are perpendicular to the line $x - y + 4 = 0$

- (A) $y = -x + 3\sqrt{3}$ (B) $y = x - 3\sqrt{3}$
(C) $y = -x \pm 2$ (D) None of these

Q.30 The line $y = x + 2$ touches the hyperbola $5x^2 - 9y^2 = 45$ at the point-

- (A) (0, 2) (B) (3, 1)
(C) $(-9/2, -5/2)$ (D) None of these

ANSWER KEY

Que.	1	2	3	4	5	6	7	8	9	10
Ans.	B	A	B	C	A	B	A	C	B	C
Que.	11	12	13	14	15	16	17	18	19	20
Ans.	A	C	A	C	A	D	C	C	C	A
Que.	21	22	23	24	25	26	27	28	29	30
Ans.	D	C	B	C	D	B	A	B	A	C